

# CIRCULAR DEPENDENCY: TREATMENT EFFECTIVENESS EVALUATION, INSTRUMENT VALIDATION AND PERFORMANCE APPRAISAL

**Chong Ho Yu, Samuel A. DiGangi, Angel Jannasch, & Barbara Ohlund Arizona State University  
Chong Ho Yu, Instruction and Research Support 0101, Arizona State University, Tempe AZ 85287**

**Keywords:** Treatment effectiveness, instrument validation, performance appraisal, power analysis

## Introduction

Psychological and educational research often is focused on treatment outcomes. Appropriate interpretation of treatment outcomes is based primarily on: (a) studying the efficacy of treatment, (b) the validity and reliability of instrumentation, and (c) obtaining subjects who represent a normal cross-section of the desired population to ensure accurate performance appraisal.

However, in many quasi-experimental and non-experimental settings where experimental control is lacking, often each aspect mentioned above is studied simultaneously. This convolutes the focus of research as well as comprises the interpretation of results. For example, in research on Web-based instruction, test results are often used as an indicator of both the quality of instruction and the knowledge level of students. In addition, pilot studies are implemented to examine the usefulness of the treatment program and to validate the instrument based upon the same pilot results.

To address this misapplication of methods, this article discusses the differentiation of the objectives of treatment effectiveness evaluation, instrument validation, and performance appraisal. In addition, it points out the pitfalls of circular dependency, proposes the rectification of the problems inherent in circular dependency, and presents recommendations for the application of appropriate research methods.

Further, a survey result was reported to substantiate these widespread misconceptions. The data were collected via the Internet by announcing the online survey to six different ListServ groups and Newsgroups. The survey consists of five multiple-choice questions, which are related to the functions of treatment effectiveness evaluation, instrument validation, and performance appraisal (see Appendix). Thirty-four graduate students, who had taken on average 4.9 undergraduate and graduate statistics courses, responded to the survey. The respondents span across twenty-five institutions in six continents/regions (North America, South America, Europe, Asia, Africa, New Zealand), twenty-two different undergraduate majors (e.g. chemistry, English, electrical engineering, history, psychology) and eighteen different graduate majors (e.g. biology, communication, computer science, education, finance, industrial engineering, statistics). Within the United States, the respondents came from eight different states. On the average, the participants answered 1.6 questions correctly.

## Consequences of the confusion

Researchers may be confused by the function of specific aspects in studies of treatment outcomes, instrument reliability and validity, as well as subjects' ability. Table 1 summarizes the differences of the three functions. Confusing these differences among a study's treatment, instruments and subjects may lead to grave consequences.

Table 1. Differences of treatment effectiveness evaluation, instrument validation, and performance appraisal.

| <b>Target</b>     | <b>Type</b>                        | <b>Objective</b>   | <b>Source of variation</b>               | <b>Sample size determination</b> |
|-------------------|------------------------------------|--|--|----------------------------------|
| <b>Treatment</b>  | Treatment effectiveness evaluation | To evaluate the effectiveness of a treatment such as an instructional module         | Treatment effect and experimental errors | Power, beta, effect size, alpha  |
| <b>Instrument</b> | Instrument validation              | To evaluate the reliability and validity of an instrument such as a test or a survey | Instrument items                         | Stability                        |
| <b>Subjects</b>   | Performance/ Attitude appraisal    | To evaluate the performance or/and the attitude of respondents                       | Subjects' abilities and attributes       | None                             |

### Test-retest reliability and pre-post differences

As an example, a common occurrence in the field follows: A researcher administers an instrument to a group of subjects as a pretest- treatment - posttest. The correlation between the two measurements is then examined in an attempt to estimate the test-retest reliability instead of treatment effectiveness. Indeed, a dependent t-test should be performed to compute the pre-post difference, because the source of variation is due to factors other than the instrument. However, in instrument validation, the source of variation is the instrument itself (e.g. poorly written items) while in studying treatment effectiveness, the source of variation is the treatment effect and the experimental errors. The consequence here is manifested in the interpretation of the results from such a study: that the instrument is either valid or invalid, and the treatment effect either supports or does not support the hypothesis. No matter the interpretation, the method used is inappropriate, and therefore any discussion would be invalid.

The survey results indicate that this confusion exists though it may not be widespread. Question 1 was used to test the subjects' ability to distinguish test-retest reliability from pre-post differences. Thirty-two percent of the respondents failed to differentiate the two concepts.

### Sample size determination

Further confusion of studying treatment effectiveness and instrument validation is manifested in sample size requirement. In our teaching, consulting, and research experience, many students and researchers, after calculating a desirable sample size using power analysis, use the suggested sample size or less to run pilot studies for instrument validation. Apparent in this act is the failure to distinguish the sample size requirement in studying treatment effectiveness from that in instrument validation. For example, power is the probability of correctly rejecting the null hypothesis. Thus, power analysis is inherent in studying treatment effectiveness where dependent and independent variables are present. Moreover, hypothesis testing alone does not reveal how likely the result can be replicated in other studies (Thompson, 1996). In other words, stability across samples, which is a focus of instrument validation, is not an issue in sample size determination for studying treatment effectiveness.

In contrast, instrument validation requires no distinction between dependent and independent variables, and there is no null hypothesis to be rejected. The sample size criterion for instrument validation is stability rather than power. To be specific, the larger the sample size, the more likely that the instrument can be applied to different samples. To achieve this stability, a very large sample size is necessary. For example, in factor analysis, which is a procedure of

loading items into latent constructs, 300 subjects are considered a small sample (Wolins, 1995). It is not unusual for a test developer to use as many as 5000 subjects for instrument validation (Potter, 1999). But a treatment effectiveness study with 300-5000 subjects may be considered being overpowered in power analysis. It is apparent, then, that using the results of a single power analysis to determine sample size to study treatment efficacy and instrument validation becomes problematic, and may lead to erroneous, yet over-confident conclusions.

Question 2 and 3 were used to test the subjects' knowledge on sample size determination. In Question 2, Seventy-six percent of respondents were confused by the criteria of determining sample size for treatment effectiveness study and instrument validation. Eight-two percent of responses to question 3 were incorrect. It is evident that the majority did not understand the purpose of power analysis.

Performance/attitude appraisal is less problematic. In appraisals, the conclusion is made to individuals. Even if there is only one subject, the judgment is still valid to that particular person, and therefore sample size determination is not needed.

### Circular dependency

Last but not least, this confusion may lead to the logical fallacy of circular dependency. There are two aspects of circular dependency in classical test theory. The first is the circular dependency between the theoretical constructs and the data; the second is the circular dependency between the instrument and the subjects.

First, when Cronbach and Meehl (1955) proposed the concept of construct validity, they maintained that hypothetical constructs drive the nature of data collection. For instance, when we have a theory about "social presence on the Internet," the questions and the possible choices for answers in the instrumentation will be framed within the theoretical model. In turn, the data resulting from the administration of the instrument are then used to revise the theory itself. Further, in studying treatment effectiveness, the treatment is developed based on the theory. In turn, the data are used to confirm or disconfirm the treatment effectiveness, and eventually, the theory behind the treatment. This circular dependency may be viewed as a positive feedback loop if the theory and the treatment are continuously refined by appropriately analyzing data. However, what if the research starts with terribly incorrect theoretical constructs? In this case, the data may give the right answer to the wrong question.

Embedded within the first circular dependency is as second: Fan (1998) pointed out that in classical test theory, the quality of an instrument is evaluated based upon the tester responses. At the same time, the statistics of examinees are dependent on the quality of

the test items. In other words, in studying instrument validity and reliability, test responses used to validate an instrument are also dependent upon a certain degree of the appropriate construction of that instrument. But what if the initial instrument is terribly constructed, which may be resulted from a terribly misconceived construct? The two types of circular dependency are illustrated in Figure 1:

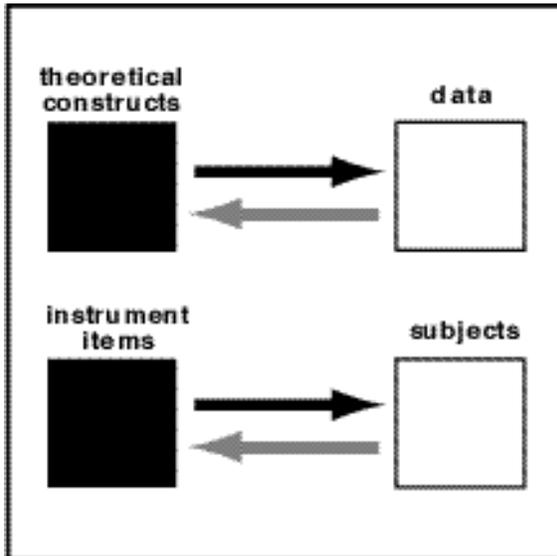


Figure 1. Two types of circular dependency

These two types of circular dependency are amplified when the three types of evaluation are not clearly delineated and are mistakenly run in parallel. The relationship between the subjects and the instrument, as well as that between the instrument and the treatment can be circular: The instrument is validated by the user input, treatment efficacy determined by the instrument results, and the final results used to determine the quality of students. By the same token, the usefulness of the treatment is judged by the learners' test performance, and later students' abilities are measured by how much they have learned from the treatment, as indicated by the test scores. To rectify this situation, our proposed guideline is simple: Researchers must know two before knowing the third.

**Rectification of the inherent problems in circular dependency**

Because of the inter-dependency among the treatment, the instrument, and the subjects, certain assumptions must be made or certain knowledge must be obtained in order to justify an assertion to either one of them:

1. Given that the treatment is effective and the instrument is valid, the evaluator is able to make a judgment about students' knowledge
2. Given that the treatment is effective and the subjects have the requisite characteristics, the evaluator can find out whether the instrument is valid or not.
3. Given that the learners are ready to learn and the instrument is valid, the evaluator can determine whether the treatment is effective or not.

In other words, one must know or assume the quality of at least two elements in order to unveil the third unknown. Therefore, problems arise when there are two or more unknown elements. When all of them are unknown, no conclusion can be made to the treatment, the instrument, or the subject. In the survey, question 5 addresses this problem. Only nine percent of respondents gave the correct answer.

Many researchers commit a common logical fallacy by asserting that "If the treatment works, the test scores are high. Thus, if the test scores are high, then the treatment works." The notation of this logical fallacy is: "If P then Q, therefore if Q then P." The first statement (If P then Q), which is called "Modus ponens" (Hurley, 1988), is a valid inference. But the second one (if Q then P) is considered the fallacy of affirming the consequent (Kelley, 1998). Put it in a concrete example: The statements that "if it rains, the ground is wet. If the ground is wet, it rains" are considered invalid. To infer from Q to P (a wet ground to raining), one must rule out other plausible rival explanations such as the city custodians are cleaning the street, an underground water pipe explodes, and so on. In other words, the fallacy of affirming the consequence occurs when "ruling out" procedures are absent. By the same token, in research it is dangerous to infer from the result (Q) such as test scores to the cause (P) without ruling out competing explanations. In the survey, question 4 tests the subjects' knowledge of logical fallacy. Fifty-six percent of participants failed to give the right answer. The following scenarios demonstrate how competing explanations create uncertainties.

Scenario 1

If the evaluator knows nothing or very little about the treatment and the instrument, but he is positive that the subjects are students who are ready to learn the content, what could be inferred from a low mean score? Figure 2 pictorially illustrates this scenario:

|           |            |          |
|-----------|------------|----------|
| ?         | ?          | ✓        |
| Treatment | Instrument | Subjects |

Figure 2. The treatment and instrument qualities are unknown.

In this scenario, there are three possible explanations: either the treatment is very poor and thus the students failed to acquire the knowledge, the test is poorly written and thus are incapable of reflecting their knowledge, or both. Since there are several competing explanations, any inference made from the result to the cause would be invalid.

Bias in Test of Economic Literacy (TEL) is a good example to elucidate the above scenario. TEL is a validated instrument and widely used in many research studies for assessing the knowledge level of economics. Using Differential Item Functioning (DIF), Walstad, W. B. and Denise (1997) found that some items in TEL are biased against female students even if the men and women who took the exam have the same skill levels in economics. Without this knowledge about the instrument, the gender difference may be mistakenly attributed to the treatment rather than to the instrument. This finding regarding TEL is built upon the fact that the skill level of one group is comparable to that of the other. Different groups tend to respond differently to the same item because of cognitive abilities and other non-biased factors. Thus, understanding the instrument and the subjects plays a crucial role in unmasking the nature of this gender effect.

Scenario 2

If the evaluator knows nothing or very little about the treatment and the students, but he adopts a validated instrument, what does a low average score of the students mean? Figure 3 illustrates this scenario:

|           |            |          |
|-----------|------------|----------|
| ?         | ✓          | ?        |
| Treatment | Instrument | Subjects |

Figure 3. The treatment and subjects' qualities are unknown.

Again, there are three possibilities: either the treatment is ineffective, the students are not ready, or both of the above. It is not uncommon that a low Cronbach Alpha coefficient, which is an indicator of internal consistency, occurs when a nationally accepted test is administered to a local group. If the test is too difficult to a sub-standard local group, random guessing to difficult items would lead to a low Cronbach Alpha coefficient.

Scenario 3

If the researcher has no knowledge about the learners, nor the test reliability or validity, but he employs a well-developed technology-based educational product, how could he interpret a low average test score? Figure 4 illustrates this scenario.

|           |            |          |
|-----------|------------|----------|
| ✓         | ?          | ?        |
| Treatment | Instrument | Subjects |

Figure 4. The instrument and subjects' qualities are unknown.

In this scenario, the outcome might be caused by the problems of the students (the lack of basic skills or the fear of using technology), the problems of the instrument (low reliability or insufficient validity), or both of them. If one uses a well-developed treatment and a validated instrument, there will be less uncertainties in the evaluation. In this case, a quantitative study could be applied immediately. However, educational researchers usually develop a new treatment and a customized instrument. Also, it is not unusual that a self-made test is used to evaluate both the treatment and the students concurrently. Inevitably, this approach risks circular dependency or false assumptions. Conclusions such as "the treatment works because the participants have performance gain. The participants improved their skill because of the treatment" suffer serious logical fallacies.

**Recommendations**

The following procedures are recommended for reducing the risk of making an invalid evaluation:

### Understanding subjects

Over-estimation or under-estimation of the learners' ability and readiness may lead to a conclusion of an ineffective treatment or an invalid instrument. In the context of psychotherapy, Dickson (1975) asserted, "the behavior in question must be related to client baselines, situational expectations, and peer performances. Only after this information is gathered should intervention take place." (p.379) This principle can also be applied to educational psychology. It is advisable for the evaluator to conduct an initial survey to the target audience. The assessment should be qualitative in nature. The purpose is to understand the need and readiness of the subjects. At this point numeric data may not be helpful to gain the insight pertaining to the subjects. During this process, the goal is not only to find out how much the students have already known, but also how much they do not know.

It is a common practice that a pretest is administered prior to the treatment. However, usually the purpose of the pretest is not to understand the subjects. Rather it is directly applied to studying treatment effectiveness. i.e. The pretest scores is used as a covariate or the pretest-posttest difference is computed in a dependent t-test. To avoid threats against the validity of experiment such as the ceiling effect and regression to the mean, high and low pretest scores are simply thrown out. Very few researchers ask these questions: "Why are some people under-achievers and some over-achievers? Is it possible that those so-called 'over-achievers' are 'normal' but all the rest are substandard students who are not ready for the treatment?"

### Instrumentation

It is a common practice that evaluators use another validated instrument as a reference for developing the customized instrument, and also run several pilot studies to revise the instrument. However, the researcher should be aware that how the theoretical constructs are formulated dictates how the instrument is written. Observing and interviewing subjects in an unstructured fashion may help the researcher to discover new constructs and lead the study in a new direction. As Messick (1980, 1988) pointed out, construct validation is a never-ending process. New findings or new credible assumptions may lead to a change in construct interpretation, theory, or measurement.

### Refining treatment

The developer should use another well-established treatment as a model for developing the new treatment, and beta test the treatment using the think-aloud protocol (Ericsson, 1993; Ericsson & Smith, 1991). The think aloud protocol, also known as the mental protocol and the concurrent protocol, is a data collection technique in which the subject verbally expresses

whatever he is thinking when he performs a task. This technique is particularly useful when the treatment involves complex mental processing.

As mentioned before, a misconceived theoretical construct could lead to a treatment addressing the wrong research question and an instrument evaluating the misdirected target. A think aloud protocol can help the researcher to gain insight of a complex mental process and thereby develop appropriate constructs. For instance, in a study regarding teaching children using object-oriented languages to program LEGO-made robots (Instructional Support Group, 1999), the objective of the treatment is to enhance problem-solving skills. In this context, the specific problem solving skill is defined as the ability of modularizing a task and restructuring the relationships among objects (components) to form a coherent and functioning model (Kohler, 1925; 1969). The designs of the treatment and the instrument are difficult because problem-solving in terms of restructuring objects is an abstract theoretical construct, which involves a complex mental model. In this situation, the think aloud protocol can be useful to understand the mental construct.

It is important to note that in research the ultimate goal is concerned with broader concepts rather than a particular software package or a product created by the software (Yu, 1998). For example, the evaluator is interested in not only the instructional value of a Website, but also the concepts of "hypermedia" and "hypertext." Thus, the refinement of the treatment must align with the intended media features. More importantly, the media features must be mapped to the mental constructs to be studied. If the treatment is packed with many other features that are unrelated to the research objectives, the subsequent evaluation may be biased.

### **Conclusion**

The differences among treatment effectiveness study, instrument validation, and performance appraisal may lead to confusion between the use of test-retest reliability and dependent t-tests for pre-post difference. Also, these elements may give a false sense of security in sample size determination when the goals of power and stability are not differentiated. More importantly, a serious logical fallacy of circular dependency may result from the failure to rule out rival explanations. This paper is an attempt to clarify these misconceptions and to provide practical solutions.

### **Acknowledgements**

Special thanks to Ms. Joseph Corrigan for reviewing this paper.

## References

- Cronbach, L. J., & Meehl, P. E. (1955). Construct validity in psychological tests. Psychological Bulletin, 52, 281-302.
- Dickson, C. R. (1975). Role of assessment in behavior therapy. In P. McReynolds (Ed.), Advances in psychological assessment (Vol. 3). San Francisco, CA: Jossey-Bass.
- Ericsson, K. A. (1993). Protocol analysis: Verbal reports as data. Cambridge, MA: MIT Press.
- Ericsson, K. A., & Smith, J. (1991). Toward a theory of expertise. New York: Cambridge University Press.
- Fan, X. (1998). Item response theory and classical test theory: An empirical comparison of their item/person statistics. Educational & Psychological Measurement, 58, 357-384.
- Hurley, P. J. (1988). A concise introduction to logic. Belmont, CA: Wadsworth Publishing Company.
- Instruction Support Group. (1999) The Conexiones project. [On-line] Available: <http://conexiones.asu.edu>.
- Kelley, D. (1998). The art of reasoning (3<sup>rd</sup> ed.). New York: W. W. Norton & Company.
- Kohler, W. (1925). The mentality of apes. New York: Harcourt.
- Kohler, W. (1969). The task of Gestalt psychology. Princeton, N. J.: Princeton University Press.
- Messick, S. (1980). Test validity and the ethics of assessment. American Psychologist, 35, 1012-1027.
- Messick, S. (1988). The once and future issues of validity: Assessing the meaning and consequence of measurement. In H. Wainer & H. I. Vraun (Eds.) Test validity (pp.33-45). Hillsdale, NJ: Lawrence Erlbaum Associates, Publishers.
- Potter, C. C. (1999). Measuring children's mental health functioning: Confirmatory factor analysis of a multidimensional measure. Social Work Research, 23, 42-55.
- Thompson, B. (1996). AERA editorial policies regarding statistical significance testing: Three suggested reforms, Educational Researcher, 25(2), 26-30.
- Walstad, W. B., & Robson, D. (1997). Differential item functioning and male-female differences on multiple-choice tests in economics. Journal of Economic Education, 28, 155-171.
- Wolins, L. (1995). A Monte Carlo study of constrained factor analysis using maximum likelihood and unweighted least squares, Educational & Psychological Measurement, 55, 545-559.
- Yu, C. H. (1998). Media evaluation. [On-line] Available: <http://seamonkey.ed.asu.edu/~alex/teaching/assessment/media.html>.

## Appendix

- Q1: A researcher administers an instrument to a group prior to the experiment, then he administers the same test again after the experiment. What kind of statistics should he compute for the test data?
- test-retest reliability
  - alternate form
  - dependent t-test for pre-post difference
  - both
- Q2: What criteria should a researcher use to determine the desirable sample size for instrument validation?
- How likely the null hypothesis can be rejected given that the null is false.
  - To what degree the response patterns can be stable across different samples
  - Both
  - None of the above
- Q3: Power analysis for determining sample size can be applied in which of the following situation(s)?
- Statistical analysis for treatment effectiveness
  - Instrument validation
  - Both
  - None of the above
- Q4: Given the statement: "If P then Q," which of the following is a valid logical deduction?
- If not Q, not P
  - If Q, then P
  - If not P, then not Q
  - All of the above are valid
- Q5: If test scores are high after subjects have been exposed to a treatment, which is more likely to be true?
- The treatment enhances learning effectively
  - The test is too easy
  - The subjects are too smart
  - (a) and (b)
  - All of the above